

Zbl 152.41201

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*On chromatic graphs* (In Hungarian)

Mat. Lapok 18, 1-4 (1967). [0025-519X]

Authors' summary: "A graph  $G$  is said to have property  $T_c$  if for every  $k$  and every  $k$  of its vertices  $x_1, \dots, x_k$  the subgraph  $G(x_1, \dots, x_k)$  spanned by the vertices  $x_1, \dots, x_k$  contains a set of independent vertices having  $ck$  elements. We show that for every  $c < \frac{1}{2}$  there is a graph  $G$  having property  $T_c$  and chromatic number  $\aleph_0$ . Clearly a graph having property  $T_{1/2}$  has chromatic number at most 2. The question is left open if for every  $m > \aleph_0$  and every  $c < \frac{1}{2}$  there is a graph  $G$  having  $m$  vertices, satisfying property  $T_c$  and of chromatic number  $m$ ."

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Classification:

05C15 Chromatic theory of graphs and maps