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*An application of graph theory to additive number theory.* (In English)

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It is proved that, if  $\mathfrak{A} = a_1 < a_2 < \dots < a_n$  is a sequence of positive integers such that no integer can be expressed as a sum  $a_i + a_j$  in more than  $k$  ways, then  $\mathfrak{A}$  is the union of  $C_1(k)n^{1/3}$   $B_2$ -sequences, a  $B_2$ -sequence being a sequence with all two-element sums distinct. On the other hand, such an  $\mathfrak{A}$  exists which is not the union of  $C_2(k)n^{1/3}$   $B_2$ -sequences. Proofs are couched in terms of hypergraphs.

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Classification:

11B83 Special sequences of integers and polynomials

11P99 Additive number theory

05C65 Hypergraphs

Keywords:

Sidon sequence; distinct two-element sums;  $B_2$ -sequences; hypergraphs