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On graphical partitions. (In English)

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For even n, let $p(n)$ denote the number of partitions of n and $G(n)$ denote the number of graphical partitions of n. A partition $\pi = (\lambda_1, \lambda_2, \ldots, \lambda_m)$ is graphical if there exists a graph with degree sequence π. The authors discuss progress and possible lines in enquiry on the questions of whether or not $\lim_{n\to\infty} G(n)/p(n)$ approaches 0, and prove two inequalities:

$$\limsup_{n\to\infty} \frac{G(n)}{P(n)} \leq .4258, \ \liminf_{n\to\infty} n^{1/2} \frac{G(n)}{P(n)} \geq \frac{\pi}{\sqrt{6}}.$$

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11B83 Special sequences of integers and polynomials
05C99 Graph theory

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