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## WIDTH-INTEGRALS AND AFFINE SURFACE AREA OF CONVEX BODIES

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**ABSTRACT.** The main purposes of this paper are to establish some new Brunn–Minkowski inequalities for width-integrals of mixed projection bodies and affine surface area of mixed bodies, together with their inverse forms.

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