



Banach J. Math. Anal. 2 (2008), no. 2, 31–41

**BANACH JOURNAL OF MATHEMATICAL ANALYSIS**

ISSN: 1735-8787 (electronic)

<http://www.math-analysis.org>

## SOME REMARKS ON THE TRIANGLE INEQUALITY FOR NORMS

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*Dedicated to Professor Josip Pečarić*

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ABSTRACT. Remarks about strengthening of the triangle inequality and its reverse inequality in normed spaces for two and more elements are collected. There is also a discussion on Fischer–Muszély equality for  $n$ -elements in a normed space. Some other estimates which follow from the triangle inequality are also presented.

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*Date:* Received: 11 April 2008; Accepted 24 April 2008.

*2000 Mathematics Subject Classification.* Primary 46B20, 46B99; Secondary 51M16.

*Key words and phrases.* Inequalities, normed space, norm inequality, triangle inequality, reversed triangle inequality, angular distance, Fischer–Muszély equality.