



Banach J. Math. Anal. 2 (2008), no. 2, 76–84

**BANACH JOURNAL OF MATHEMATICAL ANALYSIS**

ISSN: 1735-8787 (electronic)

<http://www.math-analysis.org>

## THE HARDY INEQUALITY WITH ONE NEGATIVE PARAMETER

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*Dedicated to Professor Josip E. Pečarić*

Submitted by C. Park

ABSTRACT. In this paper, necessary and sufficient conditions for the validity of the Hardy inequality for the case  $q < 0$ ,  $p > 0$  and for the case  $q > 0$ ,  $p < 0$  are derived.

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*Date:* Received: 19 February 2008; Accepted: 3 June 2008.

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2000 *Mathematics Subject Classification.* Primary 26D10, 26D15; Secondary 47B38.

*Key words and phrases.* Inequalities, Hardy-type inequalities, weights, negative powers.