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WEIGHTED INEQUALITIES AND SPECTRAL PROBLEMS

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Dedicated to Professor Lars-Erik Persson on the occasion of his 65th birthday

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ABSTRACT. It is shown that the conditions of the validity of the Hardy inequality coincide with the conditions on the spectrum of some (nonlinear) differential operators to be bounded from below and discrete.

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