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ON A JENSEN–MERCER OPERATOR INEQUALITY

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ABSTRACT. A general formulation of the Jensen–Mercer operator inequality for operator convex functions, continuous fields of operators and unital fields of positive linear mappings is given. As consequences, a global upper bound for Jensen’s operator functional and some properties of the quasi-arithmetic operator means and quasi-arithmetic operator means of Mercer’s type are obtained.

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