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## A GLIMPSE AT THE DUNKL–WILLIAMS INEQUALITY

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ABSTRACT. In this paper we survey the results on the Dunkl–Williams inequality in normed linear spaces. These are related to the geometry of normed linear spaces, the characterizations of inner product spaces, some inequalities regarding operators on Hilbert spaces and elements of Hilbert  $C^*$ -modules.

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