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## QUASI-MULTIPLIERS OF THE DUAL OF A BANACH ALGEBRA

M. ADIB<sup>1</sup>, A. RIAZI<sup>2\*</sup> AND J. BRAČIČ<sup>3</sup>

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**ABSTRACT.** In this paper we extend the notion of quasi-multipliers to the dual of a Banach algebra  $A$  whose second dual has a mixed identity. We consider algebras satisfying weaker condition than Arens regularity. Among others we prove that for an Arens regular Banach algebra which has a bounded approximate identity the space  $QM_r(A^*)$  of all bilinear and separately continuous right quasi-multipliers of  $A^*$  is isometrically isomorphic to  $A^{**}$ . We discuss the strict topology on  $QM_r(A^*)$  and apply our results to  $C^*$ -algebras and to the group algebra of a compact group.

<sup>1,2</sup> DEPARTMENT OF MATHEMATICS AND COMPUTER SCIENCE, AMIRKABIR UNIVERSITY OF TECHNOLOGY, P. O. BOX 15914, TEHRAN 91775, IRAN.

*E-mail address:* [madib@aut.ac.ir](mailto:madib@aut.ac.ir)

*E-mail address:* [riazi@aut.ac.ir](mailto:riazi@aut.ac.ir)

<sup>3</sup> IMFM, UNIVERSITY OF LJUBLJANA, JADRANSKA UL. 19, SI-1000, LJUBLJANA, SLOVENIA.

*E-mail address:* [janko.bracic@fmf.uni-lj.si](mailto:janko.bracic@fmf.uni-lj.si)

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\* Corresponding author.

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