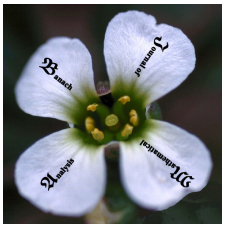

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STABILIZING ISOMORPHISMS FROM $\ell_p(\ell_2)$ INTO $L_p[0,1]$

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Abstract. Let $1 < p \neq 2 < \infty$, $\varepsilon > 0$ and let T be an isomorphism from $\ell_p(\ell_2)$ into $L_p[0,1]$. Then there is a subspace $Y \subset \ell_p(\ell_2)$, $(1+\varepsilon)$-isomorphic to $\ell_p(\ell_2)$ such that $T_{|Y}$ is an $(1+\varepsilon)$-isomorphism and $T(Y)$ is K_p-complemented in $L_p[0,1]$, with K_p depending only on p. Moreover, $K_p \leq (1+\varepsilon)\gamma_p$ if $p > 2$ and $K_p \leq (1+\varepsilon)\gamma_{p/(p-1)}$ if $1 < p < 2$, where γ_r is the L_r norm of a standard Gaussian variable.

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