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OPTIMAL RANGE THEOREMS FOR OPERATORS WITH p -TH POWER FACTORABLE ADJOINTS

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ABSTRACT. Consider an operator $T : E \rightarrow X(\mu)$ from a Banach space E to a Banach function space $X(\mu)$ over a finite measure μ such that its dual map is p -th power factorable. We compute the optimal range of T that is defined to be the smallest Banach function space such that the range of T lies in it and the restricted operator has p -th power factorable adjoint. For the case $p = 1$, the requirement on T is just continuity, so our results give in this case the optimal range for a continuous operator. We give examples from classical and harmonic analysis, as convolution operators, Hardy type operators and the Volterra operator.

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