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WEIGHTED CLASSES OF QUATERNION-VALUED FUNCTIONS

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ABSTRACT. In this paper, we define the classes $F(p, q, s)$ of quaternion-valued functions, then we characterize quaternion Bloch functions by quaternion $F(p, q, s)$ functions in the unit ball of \mathbb{R}^3 . Further, some important basic properties of these functions are also considered.

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