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## MATRIX TRANSFORMATIONS AND SEQUENCE SPACES EQUATIONS

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ABSTRACT. In this paper we study sequence spaces equations (SSE) with operators, which are determined by an identity whose each term is a sum or a sum of products of sets of the form  $\chi_a(T)$  and  $\chi_{f(x)}(T)$  where f maps  $U^+$  to itself,  $\chi$  is either of the symbols  $s, s^0$ , or  $s^{(c)}$ . Then we solve five (SSE) of the form  $\chi_a + \chi'_x = \chi'_b$ , where  $\chi, \chi'$  are either  $s^0, s^{(c)}$ , or s. We apply the previous results to the solvability of the systems  $s^0_a + s_x(\Delta) = s_b, s_x \supset s_b$  and  $s_a + s^{(c)}_x(\Delta) = s^{(c)}_b, s^{(c)}_x \supset s^{(c)}_b$ . Finally we solve the (SSE) with operators defined by  $\chi_a(C(\lambda) D_{\tau}) + s^{(c)}_x(C(\mu) D_{\tau}) = s^{(c)}_b$  where  $\chi$  is either  $s^0$ , or s.

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