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## COMPOSITION OPERATORS BETWEEN WEIGHTED BERGMAN SPACES WITH ADMISSIBLE BÉKOLLÉ WEIGHTS

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**ABSTRACT.** We study composition operators acting between weighted Bergman spaces with admissible Békollé weights. The boundedness and compactness of composition operators are characterized in terms of the generalized Nevanlinna counting function associated with the inducing map of the composition operator and the associated weight function of Bergman space. For a special case, we also give the estimate of the essential norm.

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