



Banach J. Math. Anal. 8 (2014), no. 1, 89–97

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**B**ANACH **J**OURNAL OF **M**ATHEMATICAL **A**NALYSIS

ISSN: 1735-8787 (electronic)

[www.emis.de/journals/BJMA/](http://www.emis.de/journals/BJMA/)

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## ORTHONORMAL BASES AND A STRUCTURE OF FINITE DIMENSIONAL NORMED LINEAR SPACES

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Communicated by D. Bakić

**ABSTRACT.** In this paper, we consider orthonormal bases for finite dimensional normed linear spaces which are related to Birkhoff orthogonality. We also study the relationship between orthonormal bases and a structure of finite dimensional normed linear spaces.

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*Date:* Received: 8 April 2013; Accepted: 28 April 2013.

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2010 *Mathematics Subject Classification.* Primary 46B20; Secondary 46B25.

*Key words and phrases.* Birkhoff orthogonality, orthonormal basis, normed linear space.