



Banach J. Math. Anal. 8 (2014), no. 2, 1–15

BANACH JOURNAL OF MATHEMATICAL ANALYSIS

ISSN: 1735-8787 (electronic)

www.emis.de/journals/BJMA/

COMPACT OPERATORS IN THE COMMUTANT OF ESSENTIALLY NORMAL OPERATORS

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Communicated by D. Bakić

ABSTRACT. Let T be a bounded, linear operator on a complex, separable, infinite dimensional Hilbert space H . We assume that T is an essentially isometric (resp. normal) operator, that is, $I_H - T^*T$ (resp. $TT^* - T^*T$) is compact. For the compactness of S from the commutant of T , some necessary and sufficient conditions are found on S . Some related problems are also discussed.

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Date: Received: Feb. 11, 2013; Revised: May 21, 2013; Accepted: Aug. 7, 2013.

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2010 *Mathematics Subject Classification.* Primary 47A10; Secondary 47A53, 47A60, 47B07.

Key words and phrases. Compact operator, essentially unitary (normal) operator, (essential) spectrum, functional calculus.