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## CALCULUS OF OPERATORS: COVARIANT TRANSFORM AND RELATIVE CONVOLUTIONS

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**ABSTRACT.** The paper outlines a covariant theory of operators related to groups and homogeneous spaces. A methodical use of groups and their representations allows to obtain results of algebraic and analytical nature. The consideration is systematically illustrated by a representative collection of examples.

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