

AN ANGLE METRIC THROUGH THE NOTION OF GRASSMANN REPRESENTATIVE*

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Abstract. The present paper has two main goals. Firstly, to introduce different metric topologies on the pencils (F, G) associated with autonomous singular (or regular) linear differential or difference systems. Secondly, to establish a new angle metric which is described by decomposable multi-vectors called Grassmann representatives (or Plücker coordinates) of the corresponding subspaces. A unified framework is provided by connecting the new results to known ones, thus aiding in the deeper understanding of various structural aspects of matrix pencils in system theory.

Key words. Angle metric, Grassmann manifold, Grassmann representative, Plücker coordinates, Exterior algebra.

AMS subject classifications. 15A75, 15A72, 32F45, 14M15.

*Received by the editors November 5, 2008. Accepted for publication February 5, 2009. Handling Editor: Michael J. Tsatsomeros.

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