

ABSTRACT. If the differential expressions P and L are polynomials (over \mathbb{C}) of another differential expression they will obviously commute. To have a P which does not arise in this way but satisfies $[P, L] = 0$ is rare. Yet the question of when it happens has received a lot of attention since Lax presented his description of the KdV hierarchy by Lax pairs (P, L) . In this paper the question is answered in the case where the given expression L has matrix-valued coefficients which are rational functions bounded at infinity or simply periodic functions bounded at the end of the period strip: if $Ly = zy$ has only meromorphic solutions then there exists a P such that $[P, L] = 0$ while P and L are not both polynomials of any other differential expression. The result is applied to the AKNS hierarchy where $L = JD + Q$ is a first order expression whose coefficients J and Q are 2×2 matrices. It is therefore an elementary exercise to determine whether a given matrix Q with rational or simply periodic coefficients is a stationary solution of an equation in the AKNS hierarchy.