

ABSTRACT. Let  $F$  be a closed surface. If  $i, i' : F \rightarrow \mathbb{R}^3$  are two regularly homotopic generic immersions, then it has been shown in [N] that all generic regular homotopies between  $i$  and  $i'$  have the same number mod 2 of quadruple points. We denote this number by  $Q(i, i') \in \mathbb{Z}/2$ . For  $F$  orientable we show that for any generic immersion  $i : F \rightarrow \mathbb{R}^3$  and any diffeomorphism  $h : F \rightarrow F$  such that  $i$  and  $i \circ h$  are regularly homotopic,

$$Q(i, i \circ h) = \left( \text{rank}(h_* - \text{Id}) + (n + 1)\epsilon(h) \right) \bmod 2,$$

where  $h_*$  is the map induced by  $h$  on  $H_1(F, \mathbb{Z}/2)$ ,  $n$  is the genus of  $F$  and  $\epsilon(h)$  is 0 or 1 according to whether  $h$  is orientation preserving or reversing, respectively.

We then give an explicit formula for  $Q(e, e')$  for any two regularly homotopic embeddings  $e, e' : F \rightarrow \mathbb{R}^3$ . The formula is in terms of homological data extracted from the two embeddings.