ABSTRACT. If a group acts by uniformly quasi-Möbius homeomorphisms on a compact Ahlfors *n*-regular space of topological dimension n such that the induced action on the space of distinct triples is cocompact, then the action is guasi-symmetrically conjugate to an action on the standard *n*-sphere by Möbius transformations.