ABSTRACT. We prove that every  $W^{2,2}$  isometric immersion from a convex regular domain of  $\mathbb{R}^2$  into  $\mathbb{R}^3$  can be approximated in  $W^{2,2}$ norm by smooth isometric immersions from the same domain into  $\mathbb{R}^3$