

## A STUDY ON ALMOST MATRIX SUMMABILITY OF FOURIER-JACOBI SERIES

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**Abstract.** In this paper, a quite new theorem on almost summability of Fourier-Jacobi series has been established. Our theorem extends and generalizes all previously known results of this line of work.

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