

## BOUNDED LINEAR OPERATORS ON FINITE DIMENSIONAL PROBABILISTIC NORMED SPACES

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**Abstract.** Probabilistic normed spaces were introduced by Šerstnev and have been redefined by Alsina, Schweizer, and Sklar. In this paper, we obtain some conditions under which linear operators on finite dimensional probabilistic normed spaces are bounded and continuous.

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