

AVERAGING FOR FUZZY DIFFERENTIAL EQUATIONS

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Abstract. We prove and discuss averaging results for fuzzy differential equations. Our results generalize previous ones.

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