

## TOPICS

- (1) Mersenne Primes and Perfect Numbers  
[Sil1] Chapters 14 and 15
- (2) Primitive roots  
[Sil1] Chapters 25, 26 and 27
- (3) Quadratic Reciprocity  
[Sil1] Chapters 21 and 22
- (4) Which primes and which numbers are sums of 2 squares?  
[Sil1] Chapters 23 and 24
- (5) The Gaussian Integers  
[Sil1] Chapter 34
- (6) The descent, the equation  $X^4 + Y^4 = Z^4$  and other equations  
[Sil1] Chapter 28
- (7) Square and Triangular Numbers, and Pell's Equations  
[Sil1] Chapters 29 and 30
- (8) Fibonacci's sequence  
[Sil1] Chapter 37
- (9) Diophantine Approximation and Pell's Equations  
[Sil1] Chapters 31 and 32
- (10) Irrational and Transcendental Numbers  
[Sil1] Chapter 35
- (11) Transcendence of  $e$   
[HW] Chapter 11.13
- (12) Elliptic curves in Legendre Form and the group structure  
[Ser] Chapter 36
- (13) The weak-Mordell Theorem implies the Mordell Theorem.  
[Sil2] Chapter VIII parts 3,4,5.

## REFERENCES

- [Sil1] J. Silverman, *A friendly introduction to Number Theory*  
[Sil2] J. Silverman, *The Arithmetic of Elliptic Curves*  
[HW] G. Hardy and E. Wright, *An Introduction to the Theory of Numbers*  
[Ser] E. Sernesi, *Geometria 1*